

# Study guide: Scientific software engineering; wave equation model

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Oct 20, 2015

## Migrating loops to Cython

- Vectorization: 5-10 times slower than pure C or Fortran code
- Cython: extension of Python for translating functions to C
- Principle: declare variables with type

## Declaring variables and annotating the code

Pure Python code:

```
def advance_scalar(u, u_1, u_2, f, x, y, t,
                 n, Cx2, Cy2, dt2, D1=2, D2=1):
    Ix = range(0, u.shape[0]); Iy = range(0, u.shape[1])
    for i in Ix[1:-1]:
        for j in Iy[1:-1]:
            u_xx = u_1[i-1, j] - 2*u_1[i, j] + u_1[i+1, j]
            u_yy = u_1[i, j-1] - 2*u_1[i, j] + u_1[i, j+1]
            u[i, j] = D1*u_1[i, j] - D2*u_2[i, j] + \
                Cx2*u_xx + Cy2*u_yy + dt2*f(x[i], y[j], t[n])
```

- Copy this function and put it in a file with .pyx extension.
- Add type of variables:
  - function(a, b) → cpdef function(int a, double b)
  - v = 1.2 → cdef double v = 1.2
  - Array declaration:  
np.ndarray[np.float64\_t, ndim=2, mode='c'] u

## Cython version of the functions

```
import numpy as np
cimport numpy as np
cimport cython
ctypedef np.float64_t DT # data type

@cython.boundscheck(False) # turn off array bounds check
@cython.wraparound(False) # turn off negative indices (u[-1,-1])
cpdef advance(
    np.ndarray[DT, ndim=2, mode='c'] u,
    np.ndarray[DT, ndim=2, mode='c'] u_1,
    np.ndarray[DT, ndim=2, mode='c'] u_2,
    np.ndarray[DT, ndim=2, mode='c'] f,
    double Cx2, double Cy2, double dt2):

    cdef int Nx, Ny, i, j
    cdef double u_xx, u_yy
    Nx = u.shape[0]-1
    Ny = u.shape[1]-1
    for i in xrange(i, Nx):
        for j in xrange(i, Ny):
            u_xx = u_1[i-1, j] - 2*u_1[i, j] + u_1[i+1, j]
            u_yy = u_1[i, j-1] - 2*u_1[i, j] + u_1[i, j+1]
            u[i, j] = 2*u_1[i, j] - u_2[i, j] + \
                Cx2*u_xx + Cy2*u_yy + dt2*f[i, j]
```

Note: from now in we skip the code for setting boundary values

## Visual inspection of the C translation

See how effective Cython can translate this code to C:

```
Terminal> cython -a wave2D_u0_loop_cy.pyx
```

Load wave2D\_u0\_loop\_cy.html in a browser (white lines indicate code that was successfully translated to pure C, while yellow lines indicate code that is still in Python):

```
for i in range(1, u.shape[0]-1):
    for j in range(1, u.shape[1]-1):
        u_xx = u_1[i-1, j] - 2*u_1[i, j] + u_1[i+1, j]
        u_yy = u_1[i, j-1] - 2*u_1[i, j] + u_1[i, j+1]
        u[i, j] = D1*u_1[i, j] - D2*u_2[i, j] + \
            Cx2*u_xx + Cy2*u_yy + dt2*f(x[i], y[j], t[n])
```

Can click on wave2D\_u0\_loop\_cy.c to see the generated C code..

## Building the extension module

- Cython code must be translated to C
- C code must be compiled
- Compiled C code must be linked to Python C libraries
- Result: C extension module (.so file) that can be loaded as a standard Python module
- Use a setup.py script to build the extension module

```
from distutils.core import setup
from distutils.extension import Extension
from Cython.Distutils import build_ext

cymodule = 'wave2D_u0_loop_cy'
setup(
    name=cymodule,
    ext_modules=[Extension(cymodule, [cymodule + '.pyx'],)],
    cmdclass={'build_ext': build_ext},
)
```

```
Terminal> python setup.py build_ext --inplace
```

## Calling the Cython function from Python

```
import wave2D_u0_loop_cy
advance = wave2D_u0_loop_cy.advance

for n in It[1:-1]:
    # time loop
    f_a[:, :] = f(xv, yv, t[n]) # precompute, size as u
    u = advance(u, u_1, u_2, f_a, x, y, t, Cx2, Cy2, dt2)
```

Efficiency:

- $120 \times 120$  cells in space:
  - Pure Python: 1370 CPU time units
  - Vectorized numpy: 5.5
  - Cython: 1
- $60 \times 60$  cells in space:
  - Pure Python: 1000 CPU time units
  - Vectorized numpy: 6
  - Cython: 1

## Migrating loops to Fortran

- Write the advance function in pure Fortran
- Use f2py to generate C code for calling Fortran from Python
- Full manual control of the translation to Fortran

## The Fortran subroutine

```
subroutine advance(u, u_1, u_2, f, Cx2, Cy2, dt2, Nx, Ny)
integer Nx, Ny
real*8 u(0:Nx,0:Ny), u_1(0:Nx,0:Ny), u_2(0:Nx,0:Ny)
real*8 f(0:Nx,0:Ny), Cx2, Cy2, dt2
integer i, j
Cf2py intent(in, out) u

C Scheme at interior points
do j = 1, Ny-1
  do i = 1, Nx-1
    u(i,j) = 2*u_1(i,j) - u_2(i,j) +
    & Cx2*(u_1(i-1,j) - 2*u_1(i,j) + u_1(i+1,j)) +
    & Cy2*(u_1(i,j-1) - 2*u_1(i,j) + u_1(i,j+1)) +
    & dt2*f(i,j)
  end do
end do
```

Note: Cf2py comment declares u as input argument and return value back to Python

## Building the Fortran module with f2py

```
Terminal> f2py -m wave2D_u0_loop_f77 -h wave2D_u0_loop_f77.pyf \
--override-signature wave2D_u0_loop_f77.f
Terminal> f2py -c wave2D_u0_loop_f77.pyf --build-dir build_f77 \
-DF2PY_REPORT_ON_ARRAY_COPY=1 wave2D_u0_loop_f77.f
```

f2py changes the argument list (!)

```
>>> import wave2D_u0_loop_f77
>>> print wave2D_u0_loop_f77.__doc__
This module 'wave2D_u0_loop_f77' is auto-generated with f2py...
Functions:
  u = advance(u,u_1,u_2,f,cx2,cy2,dt2,
             nx=(shape(u,0)-1),ny=(shape(u,1)-1))
```

- Array limits have default values
- Examine doc strings from f2py!

## How to avoid array copying

- Two-dimensional arrays are stored row by row in Python and C
- Two-dimensional arrays are stored column by column in Fortran
- f2py takes a copy of a numpy (C) array and transposes it when calling Fortran
- Such copies are time and memory consuming
- Remedy: declare numpy arrays with Fortran storage

```
order = 'Fortran' if version == 'f77' else 'C'
u = zeros((Nx+1,Ny+1), order=order)
u_1 = zeros((Nx+1,Ny+1), order=order)
u_2 = zeros((Nx+1,Ny+1), order=order)
```

Option -DF2PY\_REPORT\_ON\_ARRAY\_COPY=1 makes f2py write out array copying:

```
Terminal> f2py -c wave2D_u0_loop_f77.pyf --build-dir build_f77 \
-DF2PY_REPORT_ON_ARRAY_COPY=1 wave2D_u0_loop_f77.f
```

## Efficiency of translating to Fortran

- Same efficiency (in this example) as Cython and C
- About 5 times faster than vectorized numpy code
- > 1000 faster than pure Python code

## Migrating loops to C via Cython

- Write the advance function in pure C
- Use Cython to generate C code for calling C from Python
- Full manual control of the translation to C

## The C code

- numpy arrays transferred to C are one-dimensional in C
- Need to translate  $[i, j]$  indices to single indices

```
/* Translate (i,j) index to single array index */
#define idx(i,j) (i)*(Ny+1) + j

void advance(double* u, double* u_1, double* u_2, double* f,
             double Cx2, double Cy2, double dt2,
             int Nx, int Ny)
{
    int i, j;
    /* Scheme at interior points */
    for (i=1; i<=Nx-1; i++) {
        for (j=1; j<=Ny-1; j++) {
            u[idx(i,j)] = 2*u_1[idx(i,j)] - u_2[idx(i,j)] +
                Cx2*(u_1[idx(i-1,j)] - 2*u_1[idx(i,j)] + u_1[idx(i+1,j)]) +
                Cy2*(u_1[idx(i,j-1)] - 2*u_1[idx(i,j)] + u_1[idx(i,j+1)]) +
                dt2*f[idx(i,j)];
        }
    }
}
```

## The Cython interface file

```
import numpy as np
cimport numpy as np
cimport cython

cdef extern from "wave2D_u0_loop_c.h":
    void advance(double* u, double* u_1, double* u_2, double* f,
                double Cx2, double Cy2, double dt2,
                int Nx, int Ny)

@cython.boundscheck(False)
@cython.wraparound(False)
def advance_cwrap(
    np.ndarray[double, ndim=2, mode='c'] u,
    np.ndarray[double, ndim=2, mode='c'] u_1,
    np.ndarray[double, ndim=2, mode='c'] u_2,
    np.ndarray[double, ndim=2, mode='c'] f,
    double Cx2, double Cy2, double dt2):
    advance(&u[0,0], &u_1[0,0], &u_2[0,0], &f[0,0],
           Cx2, Cy2, dt2,
           u.shape[0]-1, u.shape[1]-1)
    return u
```

## Building the extension module

Compile and link the extension module with a setup.py file:

```
from distutils.core import setup
from distutils.extension import Extension
from Cython.Distutils import build_ext

sources = ['wave2D_u0_loop_c.c', 'wave2D_u0_loop_c.pyx']
module = 'wave2D_u0_loop_c.cy'
setup(
    name=module,
    ext_modules=[Extension(module, sources,
                           libraries=[], # C libs to link with
                           )],
    cmdclass={'build_ext': build_ext},
)
```

Terminal> python setup.py build\_ext --inplace

In Python:

```
import wave2D_u0_loop_c.cy
advance = wave2D_u0_loop_c.cy.advance_cwrap
...
f_a[:, :] = f(xv, yv, t[n])
u = advance(u, u_1, u_2, f_a, Cx2, Cy2, dt2)
```

## Migrating loops to C via f2py

- Write the advance function in pure C
- Use f2py to generate C code for calling C from Python
- Full manual control of the translation to C

## The C code and the Fortran interface file

- Write the C function advance as before
- Write a Fortran 90 module defining the signature of the advance function
- Or: write a Fortran 77 function defining the signature and let f2py generate the Fortran 90 module

Fortran 77 signature (note intent(c)):

```
subroutine advance(u, u_1, u_2, f, Cx2, Cy2, dt2, Nx, Ny)
Cf2py intent(c) advance
integer Nx, Ny, N
real*8 u(0:Nx,0:Ny), u_1(0:Nx,0:Ny), u_2(0:Nx,0:Ny)
real*8 f(0:Nx,0:Ny), Cx2, Cy2, dt2
Cf2py intent(in, out) u
Cf2py intent(c) u, u_1, u_2, f, Cx2, Cy2, dt2, Nx, Ny
return
end
```

## Building the extension module

Generate Fortran 90 module (wave2D\_u0\_loop\_c\_f2py.pyf):

```
Terminal> f2py -m wave2D_u0_loop_c_f2py \
-h wave2D_u0_loop_c_f2py.pyf --overwrite-signature \
wave2D_u0_loop_c_f2py_signature.f
```

The compile and build step must list the C files:

```
Terminal> f2py -c wave2D_u0_loop_c_f2py.pyf \
--build-dir tmp_build_c \
-DF2PY_REPORT_ON_ARRAY_COPY=1 wave2D_u0_loop_c.c
```

## Migrating loops to C++ via f2py

- C++ can be used as an alternative to C
- C++ code often applies sophisticated arrays
- Challenge: translate from numpy C arrays to C++ array classes
- Can use SWIG to make C++ classes available as Python classes
- Easier (and more efficient):
  - Make C API to the C++ code
  - Wrap C API with f2py
  - Send numpy arrays to C API and let C translate numpy arrays into C++ array classes